

# Quantification of Economy-wide Rebound Effects using FAVAR Models

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[www.macro-rebounds.org](http://www.macro-rebounds.org)

# ReCap

Makro-Rebounds  
begrenzen



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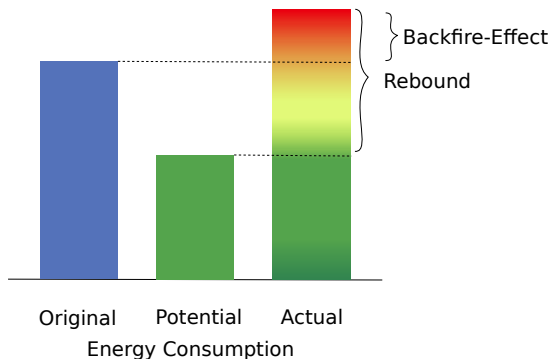
# Energy Efficiency Policy

- Save energy and money



<sup>1</sup> Source: Synthesis report on the evaluation of national notifications related to Article 14 of the Energy Efficiency Directive

# Rebound Effect

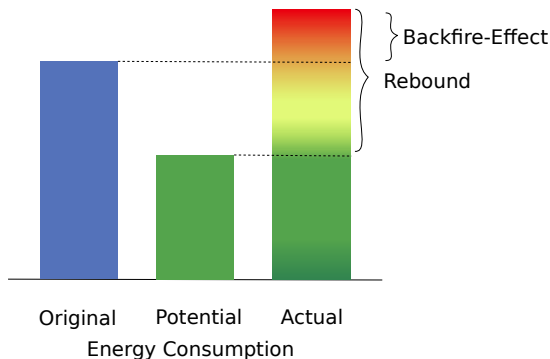


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$$\text{Rebound Effect} = 1 - \frac{\text{Actual change in Energy Consumption}}{\text{Potential change}}$$

<sup>2</sup>Own representation based on Madlener & Alcott (2011)

# Rebound Effect



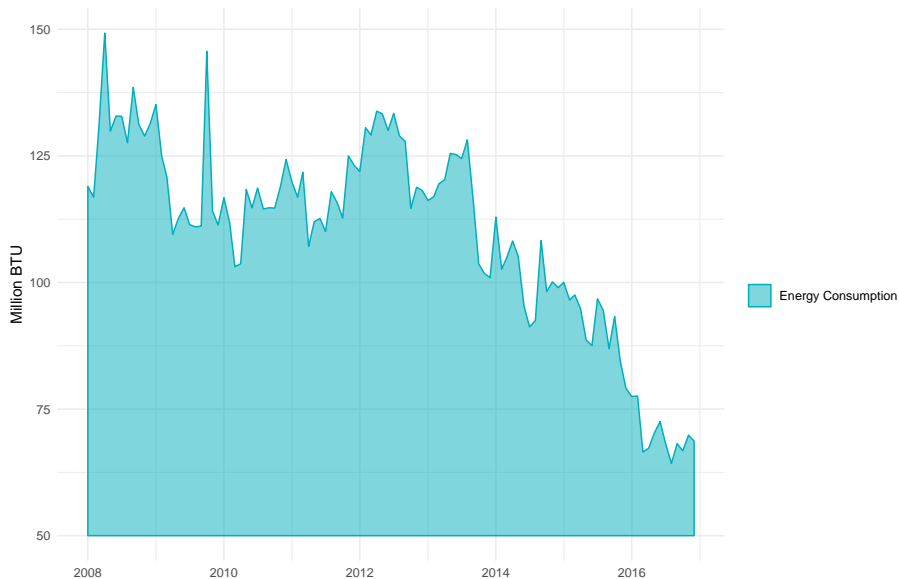
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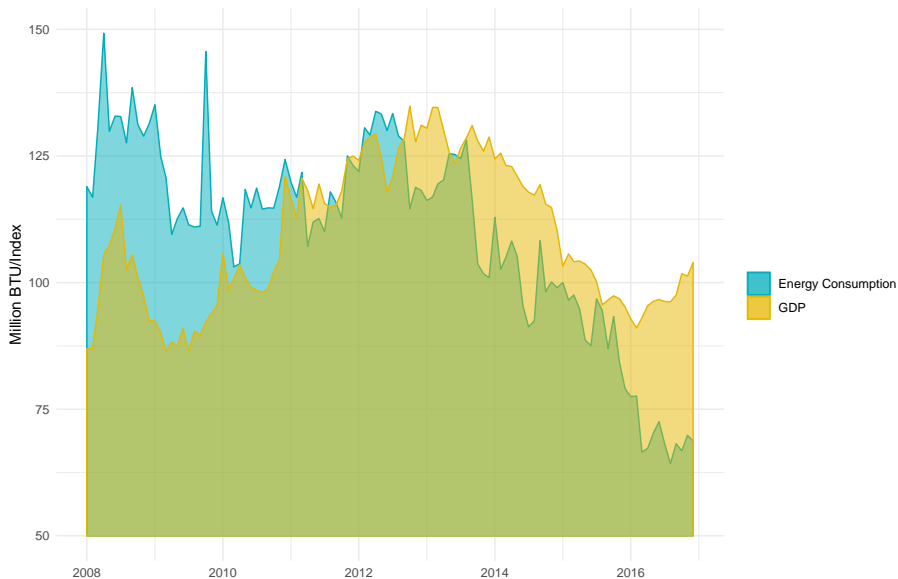
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# Simultaneity Challenge

## Decrease in Energy Consumption in the UK



# What about Causality?



# Methodology

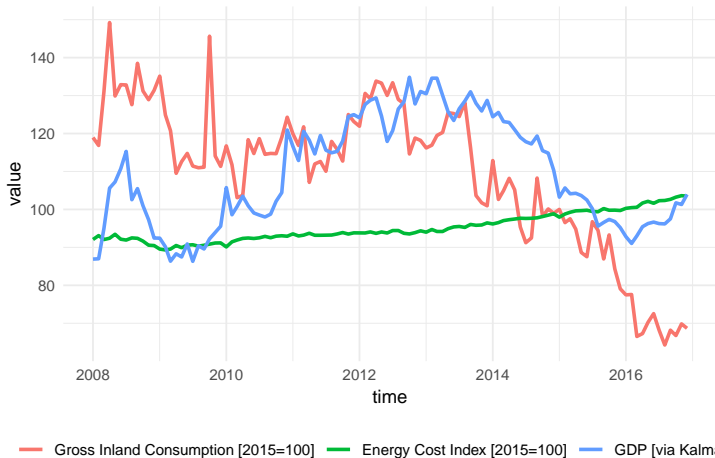
1. “Ex ante” via Partial/Computable General Equilibrium Models e.g. Turner (2013); Koesler (2013)
2. “Ex post” via econometric general equilibrium model
  - ▶ Partial equilibrium econometric estimates do not credibly identify causal effect, e.g. Saunders (2013); Orea, Llorca, and Filippini (2015)
  - ▶ **Our approach:** Structural Vector Autoregressive (SVAR) model
  - ▶ Empirical identification with minimum number of assumptions



# Methodology

Idea: Isolate energy efficiency impact on energy consumption:

$$E = f(\text{Energy Efficiency, Price, GDP, X}) \quad (1)$$



# Methodology

## SVAR Model

$$A_0 x_t = A_0 \xi_t + \sum_{i=1}^p A_0 \Pi_i x_{t-i} + \eta_t \quad (2)$$

- $x_t$  is the vector of the three variables
- $\Pi$  captures lag cross-correlations between energy use, GDP and the energy price, where  $u_t$  is a noise/shock process
- $\eta_t = A_0 u_t$  and  $\text{var}(\eta_t) = 1$
- $A_0$  captures contemporaneous effects of the endogenous variables on each other → **Identification problem**

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# Identification Problem

Data-driven Independent Component Analysis (ICA) techniques to estimate  $A_0$



3

<sup>3</sup> Source: <https://www.deichstube.de>

# Data for Europe

- Monthly data from January 2008 to December 2016
- Gross inland energy consumption: Quantity of energy necessary to satisfy inland consumption of the country
- Harmonized consumer price indices (Solid and liquid fuels, electricity and gas)
- Monthly GDP approximated via Kalman Filter (Uhlig (2005))

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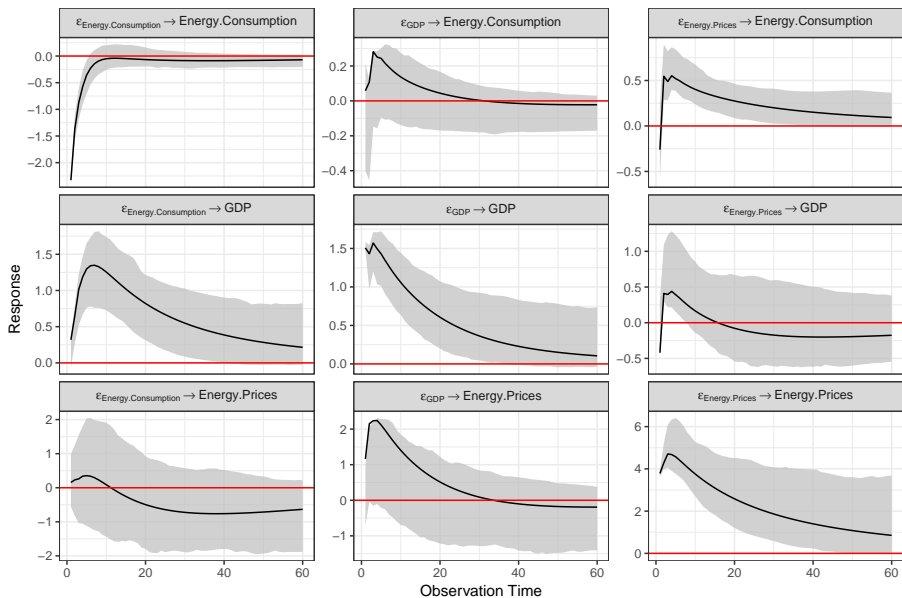
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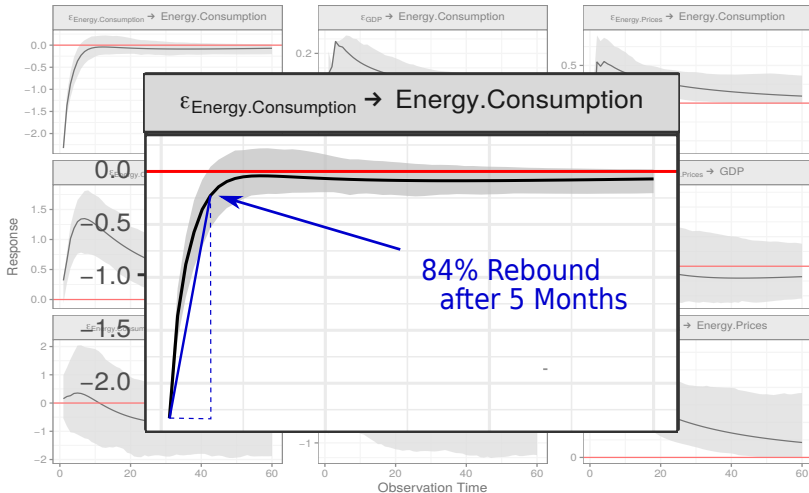
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# Impulse Response Analysis - Germany

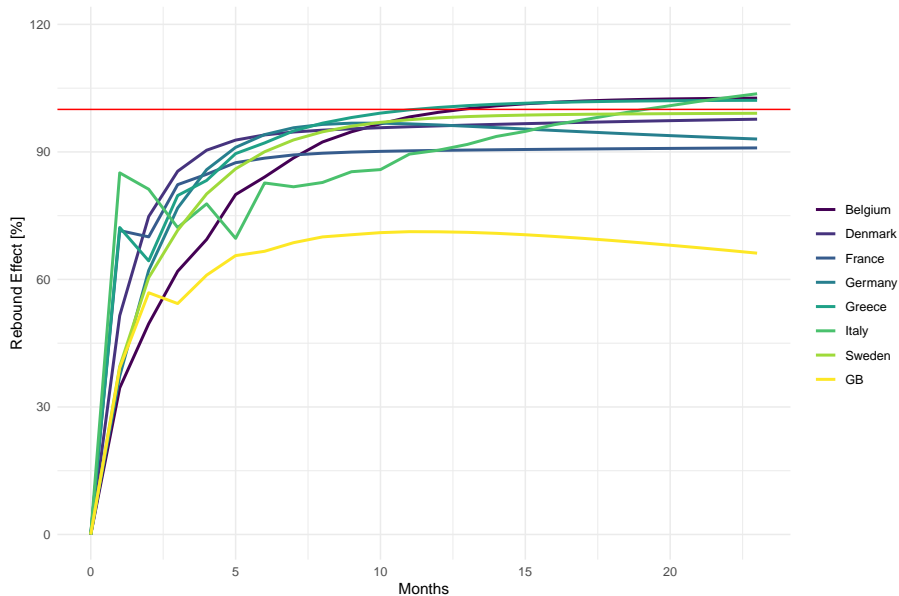


# Rebound Effect

$$R = 1 - \frac{\Delta e_i}{\Delta \hat{e}} = 1 - \frac{\text{actual change}}{\text{potential change}} \quad (3)$$



# Rebound Effects in Europe



# FAVAR - because three is not enough

- Extreme rebound effect - might have omitted variables
- Evidence that large data sets include relevant information (Stock & Watson, 2016, 2005; Bernanke, Boivin, & Eliasch, 2005)
- Idea: Use a small set of estimated factors to summarize large amount of information about the economy
  - Large monthly macroeconomic data set by OECD (MEI)
  - 1. Core variables of interest  $Y_t$  and latent Factors  $F_t$  drive the common dynamics of the large informational dataset:

$$X_t = \Lambda^f F_t + \Lambda^y Y_t + e_t$$

2. Augment system

$$\begin{bmatrix} F_t \\ Y_t \end{bmatrix} \sim VAR(d) \quad (4)$$

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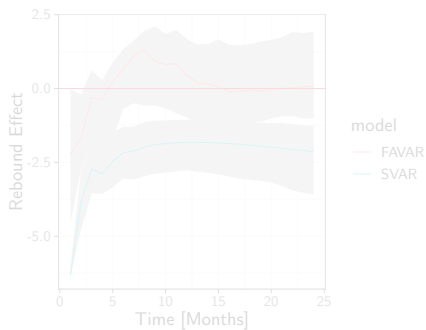
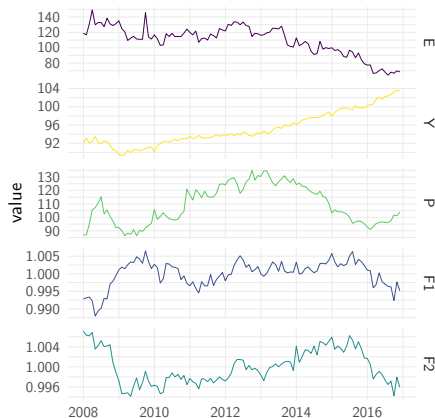
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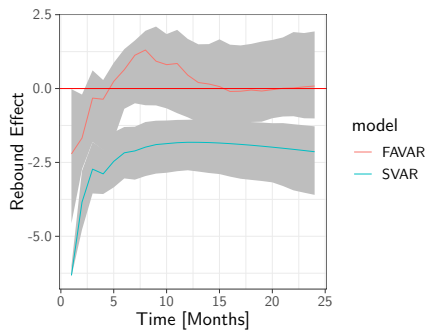
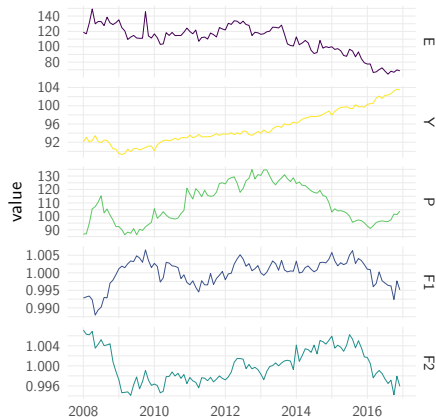
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# Factor Estimation for the UK



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# Conclusion

- Rebound effect shockingly consistent
- Approx. 100 % rebound effect in all analyzed countries after 1 year
- Future work:
  - ▶ Apply the FAVAR to all EU countries
  - ▶ Quality of Energy: Exergy/Divisia Index
  - ▶ Sectoral analysis in order to understand drivers of the rebound effect

Thank you for your attention!

# Literature I

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## Literature II

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- McCracken, M. W., & Ng, S. (2016). Fred-md: A monthly database for macroeconomic research. *Journal of Business & Economic Statistics*, 34(4), 574–589.
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## Literature III

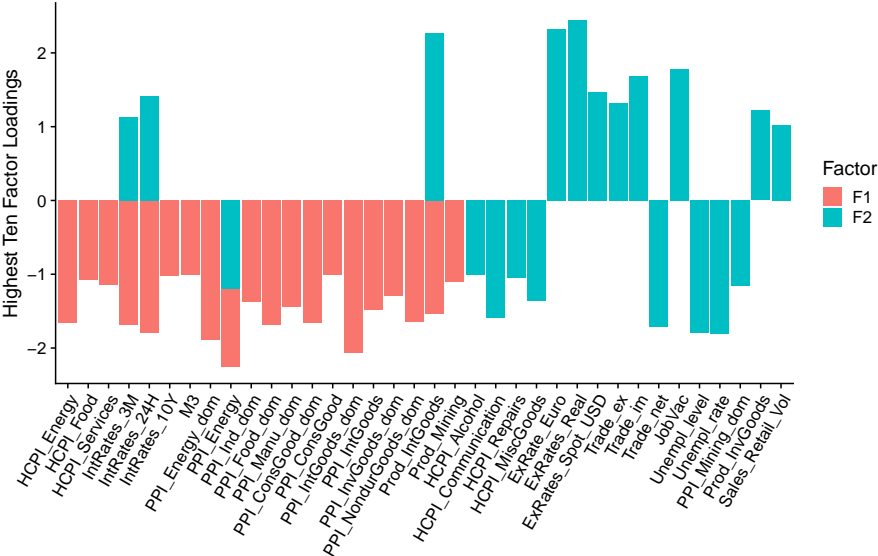
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- Turner, K. (2013). "Rebound" effects from increased energy efficiency: A time to pause and reflect. *Energy Journal*, 34(4), 25–42. doi: 10.5547/01956574.34.4.2



# Factor Estimation

- Approach: Two-step procedure (Stock & Watson, 2005)
  1. Common components,  $C_t$ , are estimated using the first principal components of  $X_t$   
→  $\hat{F}_t$  is space covered by  $C_t$  that is not covered by  $Y_t$
  2. FAVAR-equation is estimated by standard methods, with  $\hat{F}_t$
- Data: Large monthly macroeconomic data set by OECD (MEI) comparable to McCracken and Ng (2016)
  - ★ Money and Credit
  - ★ Consumption, orders, and inventories
  - ★ Import/Export
  - ★ Labour Market
  - ★ Output and Income
  - ★ Prices
  - ★ Stock Market

# Factor Loadings



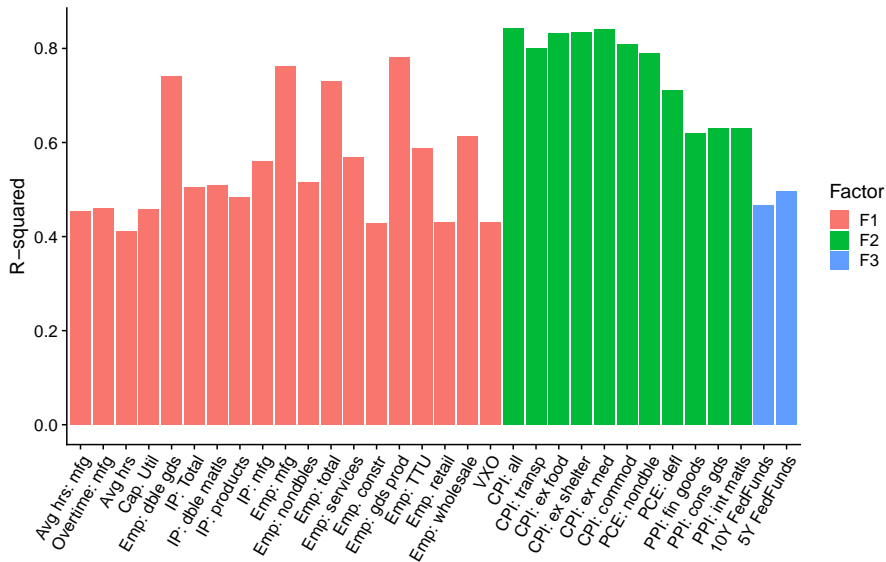
# Independent Component Analysis

Data-driven Independent Component Analysis (ICA) techniques to estimate  $A_0$

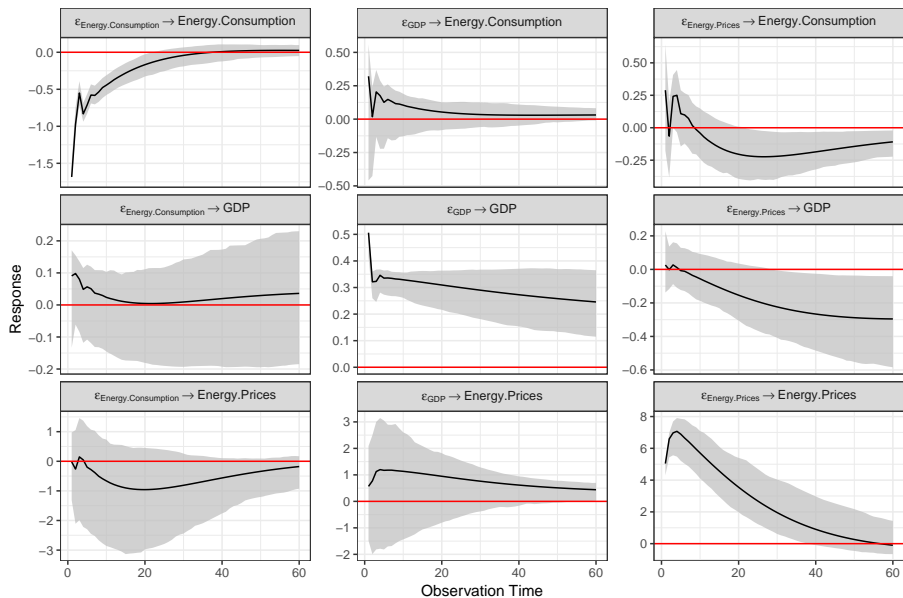
- Idea: Searching for the linear combinations of the observed data ( $u_t$ ) that are minimally dependent
  - Assumptions on elements of  $\eta_t$ :
    1. Independent - mutually and cross-sectionally
    2. Non-Gaussian - with at maximum one exception
- Invertible matrix  $A_0^{-1}$  is "almost identifiable"
- Two techniques applied by using svars-Package (Lange et al., 2018):
    1. Distance covariance approach (Matteson & Tsay, 2017)
    2. Non-Gaussian Maximum Likelihood Estimator (Lanne et al., 2017)

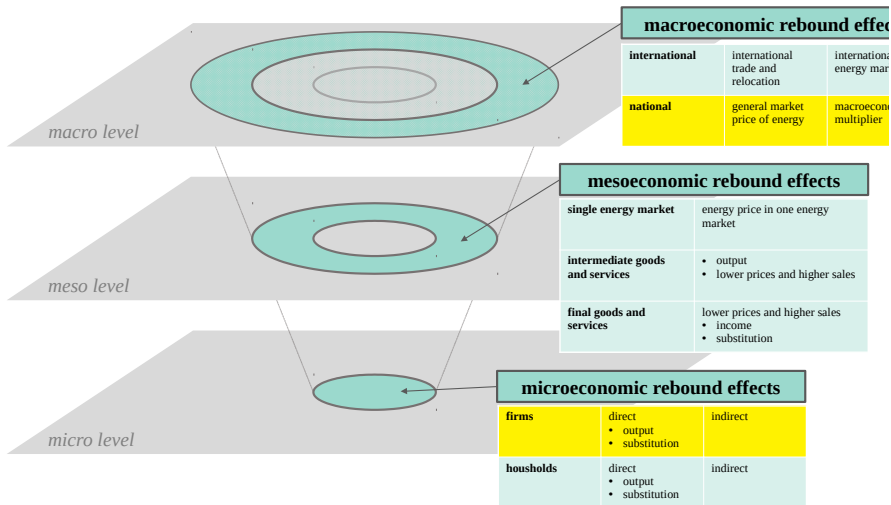
# Factor Analysis

$R^2_s > 0.4$  of regressing each variable in  $X_t$  on the three factors

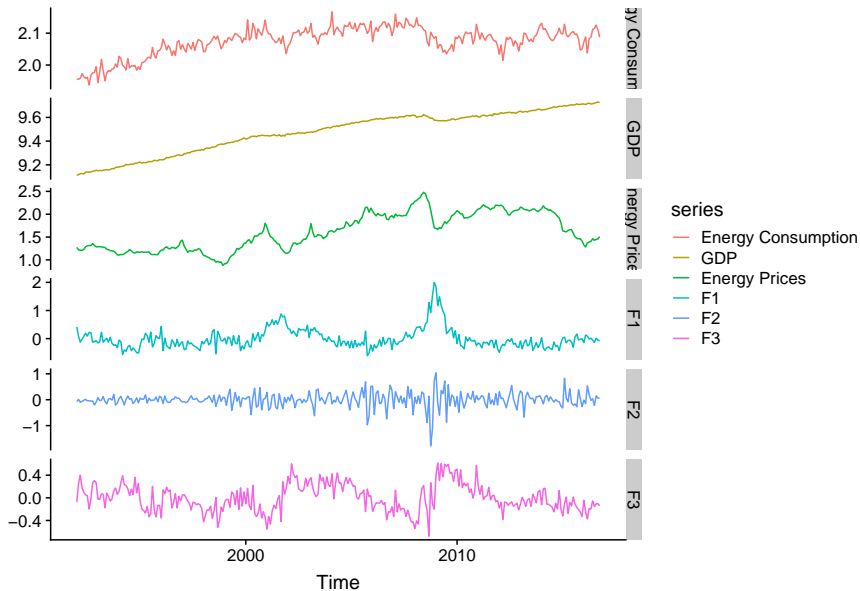


# Svar USA

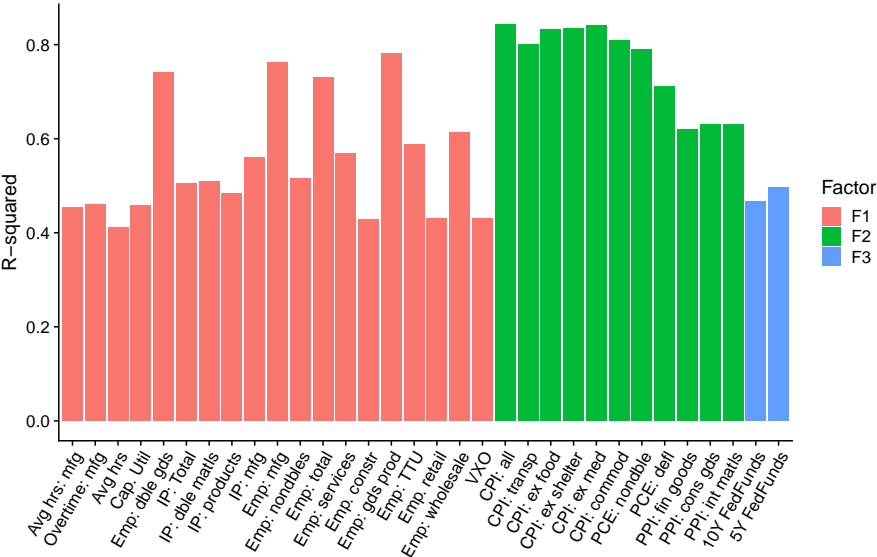




# Factor Analysis - Preliminary Results



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## Rebound effect after 5 months

	Country	X1month	X3months	X6months	X12months	CI_90
1	Belgi	49.58	69.41	88.58	100.16	[ 89.05 11
2	Germa	62.12	85.83	95.68	96.04	[ 86.9 106
3	Denma	74.80	90.40	94.68	96.31	[ 95.08 10
4	Grec	64.37	83.30	94.93	100.89	[ 89.11 10
5	Franc	70.01	84.74	89.29	90.44	[ 86.75 97
6	Italy	81.22	77.78	81.80	91.76	[ 79.15 10
7	Swede	60.42	80.12	92.82	98.31	[ 78.16 10
8	Unite	56.86	61.01	68.65	71.08	[ 55.09 82